

Examining the productiveness of failure in serious gaming

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Abstract: Serious games are games used for non-entertainment purposes, e.g. in education and training. As most serious games are highly performance-oriented and consequently include scoring systems that reward correct performances, players tend to adopt error-avoiding strategies. But thereby the players are deprived of the opportunity to learn from their mistakes. This study investigates how the differences between performance and learning can be described and formalised. To this end, it presents a computational model that takes into account the learning from mistakes. The model was empirically validated by comparing its outcomes with real-world game data. The results show that performance metrics systematically overestimate the player's actual learning at early stages in a game and underestimate these at the end. Three evaluation metrics describing the progression, efficacy and efficiency of learning show how these differences depend on the players' knowledge growth capacities and their success rates in the game. Game scoring systems should best avoid penalties for making mistakes, should reward error correction positively and should provide sufficient feedback on failure.

Keywords: serious games; games-based learning; applied games; assessment; learning; performance; simulation models; mistakes; scoring system; empirical; computational; mastery.

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Biographical notes: Wim Westera is a Full Professor in Educational Technology, in particular, Gaming and Simulation. He holds his PhD degree in Physics and Mathematics, and has worked in Educational Media Research and Development since the 1980s. He is Board Member of the Dutch Games Association, and Co-founder of the Serious Games Society and the RAGE Foundation, all dedicated to the advancement of serious gaming.

1 Introduction

Serious games are games that 'have an explicit and carefully thought-out educational purpose and are not intended to be played primarily for amusement' (Abt, 1970). Over the years, serious games have gained considerable popularity among scholars and teachers, because of their dynamic, responsive and visualised nature, capable of promoting high motivations, strong user involvement and penetrating learning experiences (Clark et al., 2016; Boyle et al., 2016; Westera, 2015). Various meta-analytic

review studies over the last decade have shown that the field of serious games research is rapidly growing, that a pile of evidence has become available about the conditions for games to be effective as a learning tool, that a variety of technical tools and platforms have become available that accommodate and simplify both game development (e.g. game engines and game authoring tools) and game deployment (e.g. tablets and mobile phones) and that games are increasingly and successfully accommodating the domain of education and training (Baptista and Oliveira, 2019; Lamb et al., 2018; Wouters and van Oostendorp, 2013; Zhonggen, 2019). Applications may range from a simple dressed-up drill-and-practice for memorisation or automation tasks, e.g. in spelling and arithmetic, to highly immersive and contextualised exercises requiring complex decision making, for instance in a simulated business context. With respect to the latter, the player in a game doesn't simply digest informational clues but essentially becomes an influential actor in the course of events, which establishes active learning along with high engagement and a sense of control, empowerment and ownership. The powerful experiences that games can provide are considered the main source of learning. Theoretical foundations of experiential learning go back to Dewey (1938) who recognised the importance of powerful experiences for learning, stating that learning should be connected with some meaningful, practical context in order to allow the learner to relate symbolic content (e.g., concepts and principles) to real-world referents. Learning from experience refers to learning by active exploration and self-direction rather than learning from direct instruction. Many related ideas and concepts have been used ever since to indicate comparable approaches, such as discovery learning (Bruner, 1961), problem-based learning (Barrows and Tamblyn, 1980), inquiry learning (Papert, 1980), experiential learning (Kolb, 1984), constructivism (Jonassen, 1991), situated learning (Lave and Wenger, 1991) and learning by doing (Schank, 1995; Aldrich, 2005), respectively. All these models put the learner at the centre of the action and emphasise discovery, exercise, inquiry, problem solving, and authentic contextual knowledge, which activate learners and help them to acquire the tacit knowledge (Polanyi, 1966) that is intrinsically bound to the actions performed. Learning from experience is the predominant pedagogical paradigm for game-based learning: players in a game engage in a problem context, they are in charge of addressing the challenges posed and they learn from the responses they obtain from the game world.

However, such experience-based learning environments are not without problems. As a consequence of the action-oriented nature of games, the player's progression in a game is directly linked with performance: new problems and new levels will open up only when the present ones are completed successfully. Accordingly, game scoring systems prompt players to perform well, that is, doing the right actions and doing them in the right way.

But unfortunately, performance in a game is not necessarily a good indicator for learning progress. Various authors (VandeWalle et al., 1999; Fisher and Ford, 1998) have pointed out the difference between performance and learning. Good performance is commonly linked with reaching milestones, the swift completion of tasks, meeting execution standards, avoiding mistakes, and reducing risks. In many respects, however, effective learning requires opposite conditions, such as having sufficient opportunities for reflection, revision, exploration, self-evaluation and notably being prepared to make mistakes (Westera, 2015). Hence, the performance orientation of games may readily conflict with the objective of learning. Game score systems, mostly being performance-based, tend to neglect the productiveness of mistakes and discourage these by assigning

penalty points. Consequently, players are drawn to activities that they are good at already as to avoid errors as much as possible, thus reducing the opportunities to learn new things.

Understanding how performances in a game (or any other learning environment) are related to the learning, requires a detailed study of the underlying processes and interactions. Principle questions to be addressed are:

- To what extent can we describe and formalise the difference between performance and learning?
- Can we quantify the difference in various conditions?
- Does it make a difference at all?
- If so, what are lessons learnt for the design of serious games and their scoring systems?

We argue that simulation models are potentially good candidates to examine these processes and to supplement existing empirical approaches, because of their orientation on micro-level processes. Accordingly, we present a computational modelling study to address the posed research questions. In the next sections, we will first resume relevant theoretical considerations with respect to the differences between performance and learning. Second, a computational model will be elaborated to describe learning and performing in complex, interactive learning environments. Next, two studies are presented. Study 1 presents an exploration of the proposed model, introduces and establishes a set of evaluation metrics, and investigates the influence of different performance success rates on learning. In study 2, the computational model is applied and tested against logged player data from a real game.

2 Performance versus learning

2.1 Learning from errors and failure

Many studies have reported the productiveness of errors and failure for learning (e.g. Mory, 2003; Mathan and Koedinger, 2005; Tjosvold et al., 2004; Ivancic and Hesketh, 2000; Keith and Frese, 2008; Calhoun et al., 2014; Gardner et al., 2015; Bridger and Mecklinger, 2014; Huelser and Metcalfe, 2012; Potts and Shanks, 2014; Radosavljević, 2015; Cattaneo and Boldrini, 2017). In a study on episodic memory Cyr and Anderson (2014) demonstrated the positive effects of learning from mistakes in conceptual tasks as compared to retrieval tasks. They conclude that conceptual mistakes are remembered well and act as ‘stepping stones’ for learning. An extensive study in nursing (Reime et al., 2016) showed that making mistakes during simulation-based team training improves the quality of patient care once the students returned to clinical practice as it made the students more vigilant. Reflecting on the errors made is crucial. Weinzimmer and Esken (2017) demonstrated the positive effects of mistake tolerance on organisational learning and performance. Simm (2005) claimed that students who are academically-strong, carry out a project effectively without major mistakes, produce a good report, but have little scope for self-critique, eventually do not outperform those

students who are academically weak, initially struggle with the project resulting in poor 'products', but learn by their mistakes and produce a good self-critique.

2.2 Negative effects of performance-based score systems

Although games for learning are essentially protected spaces that allow for failure and mistakes, the included score systems are often performance-based, which stimulates learners to demonstrate high ability and to avoid poor performance. In such contexts failure becomes a threat to success and thereby it affects self-esteem, self-confidence and motivation. The resulting self-defence reactions (Mory, 2003) may include discounting (Kelley, 1973), task avoidance, feigning boredom, and task-irrelevant actions to bolster self-image (Dweck and Legget, 1988), and learned helplessness (Seligman et al., 1968). Also, many games include designed mechanisms for inducing stress, such as time pressure or time-dependent scores, which are likely to promote hurried, shallow or incomplete processing. Risk avoidance draws players toward activities that they are good at already and make them stay away from new approaches to avoid penalty points. Performance and learning are conflicting concepts that often require opposite operational conditions and opposite attitudes. A high performance score does not necessarily indicate high learning gains. To support a learning orientation, serious games should lower the price of failure (Gee, 2003; Westera, 2019). Time constraints and penalty points should ideally be avoided, while allowing players to make mistakes, to spend sufficient time and effort, to try and retry, to reflect on attainments and to decide upon their own strategies (autonomy). To exploit the full potential of learning by doing, games need to take into account the conflicts between performance and learning and promote deep processing, reflection and the consolidation of experiences.

2.3 The performance orientation of serious games

Whatever game mechanics or game scenarios are used, game play always involves active decision taking by the players, who are challenged to find solutions to posed problems. To decide upon the quality of performance the results or solutions can then be checked against some reference standard. As a consequence, most game scoring systems are performance oriented. For instance, in business simulation games players have to run a company and strive for maximum business turnover, profit, or customer satisfaction. Performance in a ballistic challenge (physics) may be expressed by using the distance from a full hit. In a fire safety game, player performance would be expressed as the degree of agreement with prescribed safety protocols. Score systems in drill games, e.g. in arithmetic, language or geography, focusing on reproduction or automation, are fully based on correct completion, error rates or speed. Occasionally, time spent is included in the scoring system, which is disputable as such in the context of learning. In all cases, a quantitative score is defined, which is then compared with a reference to make a judgement. In its most simple form the judgement of a single game action is dichotomous: the result is either correct or incorrect, while numeric scores are assigned accordingly. Summation of the scores across all the game's challenges, eventually using different weights, yields the player's overall performance score. By its focus on completion and achievements, in-game performance assessment is essentially outcome-oriented, neglecting any process information or player history. This focus on achievements, outcomes or results, is readily associated with 'closures points', which is a

game design pattern that indicates the successful completion of a challenge, an episode, or a level (Björk and Holopainen, 2005). Hereby, performance assessment comes close to testing. Although it cannot be denied that testing may contribute to learning (the testing effect: Roediger and Karpicke, 2006), it may unnecessarily promote risk-avoiding behaviour as well as shallow and incomplete processing. Particularly in the rich and dynamic learning environments that games provide, learning from mistakes is a means too powerful to be neglected. To allow players to learn from mistakes, the history of failure should be taken into account. A failure may still contribute positively to the player's mastery of knowledge, skill or competency. In current study, the consequential inclusion of failure in assessment metrics will be investigated in detail.

3 Model starting points

3.1 A frugal representation of serious games

Serious games are complex, interactive systems composed of many interrelated game objects and their frequently changing attributes, all of which contribute to a combinatorial explosion of potential game states. Even a simple game such as tic-tac-toe (noughts and crosses) has a state space up to $3^9=19,683$ different states (neglecting any symmetries) allowing for $9!=362,880$ different trajectories through game state space. When accounting for symmetries and including games that end within 9 moves only, the number of trajectories is still 26,830 (Schaeffer, 2002). Frugality with respect to the wide range of variables that are available for describing the processes and conditions of serious gaming is dictated to avoid overfitting of an envisioned model. Rather than describing games by their numerous game states, which would account for every detailed player interaction (e.g., mouse clicks, keyboard strokes), a game is considered to provide the players with a coherent set of challenges, e.g., tasks, assignments, missions, scenes or levels that need to be passed through (Westera, 2017). Thereby a game challenge is conceived as a higher level aggregate of micro-actions, that constitute a well-defined chunk of the game scenario, it has a well-delineated scope, and its successful completion goes with a clear result or achievement that is supposed to contribute to raised mastery of knowledge or skills. Hence, a game challenge describes a part of the game rather than the whole, very similar to a learning task or learning activity in a lesson. Given the set of game activities, a serious game is represented as a network of challenges. Playing a serious game can effectively be interpreted as following a trajectory through the network of specified challenges (rather than through all possible game states).

3.2 Knowledge mastery versus performance

Serious games are designed to support the mastery of well-specified knowledge, skills or competences. For practical reasons we will use the term knowledge as a transcending, inclusive concept indicating all the things to be learned. In education and training knowledge requirements are specified as learning objectives, which serve as the formalised benchmark for assessment and certification (e.g. Anderson and Krathwohl, 2001; Bloom et al., 1956; Heller et al., 2006; Shute and Ventura, 2013). The learning objectives should not be confused with the specific goals that players are to pursue in the game (e.g. defeating enemies, collecting objects, or locating the treasure). Generally,

learning objectives are represented as a hierarchical framework of interrelated knowledge elements, while child nodes in the hierarchy have a precedence relationship with their parent nodes. The learning objectives hierarchy is static by its nature of expressing the benchmark of required learning outcomes. In general, the relationship of game activities and learning objectives entails a many-to-many relationship: each game activity may address multiple learning objectives, while at the same time each learning objective may point to multiple activities. Observed player behaviours in the activity would provide evidence for the enhanced mastery of underlying knowledge, which is generally referred to as the evidence model (Mislevy et al., 2003). Performance may well be covered by knowledge mastery, as it usually refers to the well-demonstrated mastery of certain skills or competencies. The confusion between knowledge mastery and performance arises from the fact that performance measurement is focusing on the correct execution of a task or often even the outcome only, while other dimensions of mastery (e.g., understanding, insight) are readily neglected. As a consequence, performance indicators do not fully capture the state of a player's knowledge mastery. Accordingly, we need to investigate how performance indicators relate to indicators of knowledge mastery.

4 Model development

4.1 The performance assessment model

To award the player's achievements, most serious games include a performance-based scoring system. The scores may be either manifestly communicated to the player or they are left concealed and only used to drive the evolution of the game. In its most simple form, a scoring model assigns bonus points to favourable actions. Sometimes, the systems also account for penalty points when mistakes are made. Overall performance is thus expressed as the accumulation of the bonus points assigned for successes, reduced with the penalty points assigned for failures. The assignment of scores is a discrete process that is activated only upon completion of a challenge. Consequently, performance curves are represented as discrete, stepwise functions, even though the processes of learning may be assumed to be fully continuous.

Such performance score model can be expressed as follows. Let the game be represented as a set of well-designed game challenges labelled with a natural number i and let S_i be a binary success indicator for the i -th challenge, with

$$S_i = 0 \text{ for a failure, and } S_i = 1 \text{ for success} \quad (1)$$

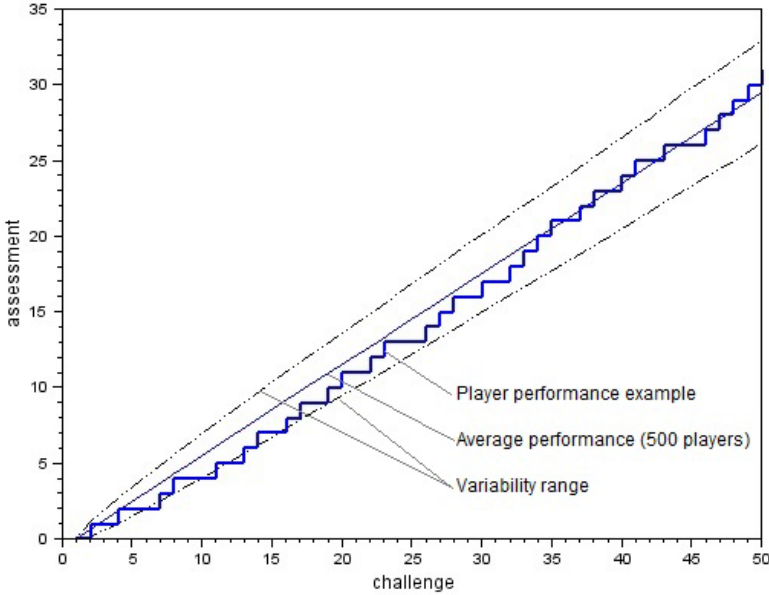
Then the cumulative performance P_i after i challenges can be written as

$$P_i = \sum_i (S_i \cdot b_i - (1 - S_i) \cdot p_i) \quad (2)$$

with b_i and p_i the bonus and penalty assigned for challenge i , respectively.

Figure 1 displays a randomly generated performance curve (dots) in accordance with such model with 50 challenges and average curves (solid) after 500 iterations (bonus points $b_i = 1$, penalty points $p_i = 0$, success rate $S_i = 0.6$).

Figure 1 A common player performance example based on a randomised sequence of 50 random successes or failures (staircase line), and the mean result of 500 iterations (thin solid line) and its variability range (dashed-dotted)



The average performance is proportional with the number of challenges, while the standard deviation is typically 7%. Changing the bonuses, penalties or success rates preserves the overall linear pattern.

A similar curve can be drawn to represent the performance score as a function of time. If D_i denotes the duration of time required to complete the i -th challenge, then the timestamp for the completion of challenge i is given by:

$$t_i = \sum_{j \leq i} D_j \tag{3}$$

Here, j is a summation index identifying all challenges addressed so far, that is $j = 1, \dots, i$. When the durations D_j are constant (each challenge requiring the same amount of time), the overall linear shape of the performance curve is preserved. Indeed, in many games, the performance score of a player will grow more or less linearly with time spent. Likewise, time may be readily replaced with effort, which would yield a similar pattern, provided that the player preserves the same intensity of effort during the game.

The linearity of these performance systems is problematic and highly unrealistic, because in practice it will become increasingly difficult to approach the level of perfection. To account for such asymptotic saturation effect we turn to a knowledge mastery model based on logistic growth.

4.2 The logistic assessment model for knowledge mastery

In many respects, the process of individual learning is all about change, growth and development. Therefore, the interplay of the individual learner and a serious game can be

considered a dynamic system, which internal structure and state continually change over time. The process of learning displays many similarities with system dynamics, which generally describes growth as a function of restricted available resources. The dynamic systems approach incorporates complex feedback mechanisms which are essentially nonlinear in nature. Systems dynamics is able to account for chaotic behaviours, instabilities, strange attractors, phase transitions and other phenomena that are associated with complexity. The complexity of learning and instruction processes certainly argues in favour of such exploration of non-linearities, as it may yield insights in the conditions for optimum knowledge growth to occur. Both internal and external variables put limitations to the growth of knowledge, which suggests that the learning of an individual readily qualifies as a system's constrained growth process. In particular, logistic functions could be used to cover the constrained growth process of learning.

The starting point for the logistic growth of the player's knowledge mastery is the following recurrent difference equation, expressed as a function of time t :

$$M_{t+\Delta t} - M_t = g \cdot M_t \cdot (M_{\max} - M_t) \cdot \Delta t \quad (4)$$

where

t is time

Δt is the increment of time

M_t is the knowledge mastery level at time t

M_{\max} is the level of ultimate perfection, and

g the unconstrained growth rate.

The logistic model complies with the proverb that 'every beginning is hard', because initial growth of knowledge mastery is proportional to the actual mastery level M_t : low mastery would lead to small growth, whereas high mastery means large growth. But the growth of mastery is also proportional to the remaining knowledge mastery gap $(M_{\max} - M_t)$, which accounts for the phenomenon that striving for perfection becomes increasingly hard when one approaches the level of perfection M_{\max} .

Again, it is assumed that the learning environment is composed of a set of separate challenges, with D_i denoting the duration of the i -th challenge (cf. equation (3)).

The main starting point is that the engagement of a player in a game challenge inherently leads to enhanced mastery, be it that the growth rate g may be different for successes and failures. To this end, we use S_i as the binary success indicator for the i -th challenge, as introduced in equation (1). Let α be the unconstrained growth rate in case of success and β the unconstrained growth rate in case of failure, then the growth rate g in equation (2) can be rewritten as g_i ,

$$g_i = \alpha \cdot S_i + \beta \cdot (1 - S_i) \quad (5)$$

Although g_i is constant during the challenge it may vary between different challenges (either equal to α or β), making it time dependent.

Equation (4) representing the knowledge mastery growth model can now be rewritten as

$$M_{t+1} - M_t = (\alpha \cdot S_i + \beta \cdot (1 - S_i)) \cdot M_t \cdot (M_{\max} - M_t) \cdot \Delta t \quad (6)$$

This equation describes the growth of the learner's mastery level, during the (small) time increment Δt . This difference equation generally can be solved analytically, be it constrained to each interval (fixed growth rate). Also, solutions can be generated through Monte-Carlo simulations, which will be presented in the next sections. The resulting mastery curves will be demonstrated to comply with the general S-shape of constrained growth given by the logistic principles: starting from a certain prior knowledge level, the knowledge mastery first grows exponentially, but gradually tends to saturate and asymptotically approach the level of perfection, as it becomes increasingly hard to improve any further.

5 Study 1: model exploration

5.1 Technical implementation

To allow for Monte-Carlo Simulations for investigating knowledge growth behaviours described by equation (6) under various conditions, the model was technically implemented in a series of Scilab programmes (www.scilab.org), while using its math functions and graphics libraries.

5.2 Baseline parameters

After preliminary exploration and testing the following parameters were set to define a baseline model with realistic growth (see Table 1). These parameters are important scaling factors and can be freely adjusted; the baseline values are chosen to restrict processing capacity as they make sure that full learning curves evolve within a limited number of iterations.

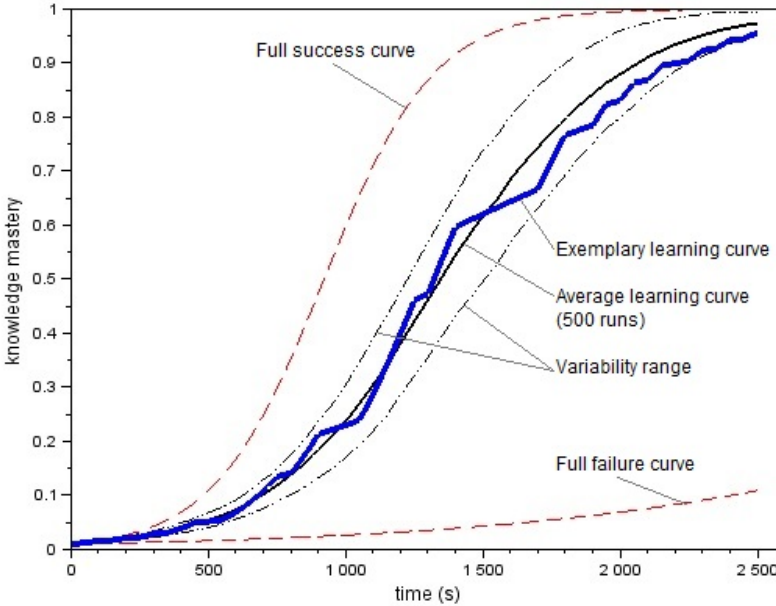
Table 1 Baseline model parameters and explanations

| <i>Parameter</i> | <i>Value</i> | <i>Explanation</i> |
|---------------------------------------|--------------|---|
| Initial knowledge mastery level M_1 | 0.01 | This is an arbitrary low prior knowledge mastery level. This value does not fundamentally influence the shape of the resulting growth curves. |
| Success growth rate α | 0.005 | A growth rate as small as this requires a substantial number of iterations to approach high mastery |
| Failure growth rate β | 0.001 | The failure growth rate was chosen to be considerably lower than the success growth rate. |
| Challenge success rate S | 0.60 | The odds of successes are 6 to 4. |
| Time increment Δt | 1 | Time is no more than a scaling factor. Each time step covers the completion of one game challenge out of an unlimited pool of challenges. |
| Challenge durations D_i | 50 | Expressed as the number of time increments Δt |
| Number of challenges n | 50 | Similar to the linear case (cf. Figure 1) |
| Total number of time steps N | 2500 | This is equal to n times D_i (number of challenges times the duration of each challenge) |

5.3 Logistic learning curves

Figure 2 displays a randomly generated growth curve and the average growth curve after 500 iterations for the baseline case. It also shows the range of the standard deviations and the two extreme cases of all successes (upper dashed line) and all failures (lower dashed line).

Figure 2 An exemplary growth curve of the baseline logistic model (bold solid), the mean baseline growth curve (thin solid) after 500 runs, the variability range (dash-dotted lines) and full success curve and full failure curve, respectively (dashed lines)



The mastery growth curve for a single run (bold solid line in Figure 2) roughly follows the logistic pattern, while it is composed of different logistic curve fragments defined by either the growth rate for successes α or for failures β .

5.4 Comparing linear and logistic assessments

The different assessment models should be compared for the very same game session. The (arbitrary) performance scale is aligned with the logistic mastery scale by setting the final linear performance score P_n (after n challenges) and the attained (logistic) mastery level M_N at the end of the game to coincide. By definition, the final mastery level is constrained to the normalised scale and any realistic level of mastery will inevitably be well below one (perfection). For a balanced comparison, three distinct assessment metrics should be evaluated: 1) the progression metric, and 2) the efficacy metric, and 3) the efficiency metric, respectively, all expressed as a normalised scalar.

5.4.1 The progression ratio

The progression ratio for logistic mastery as a function of time t is defined as

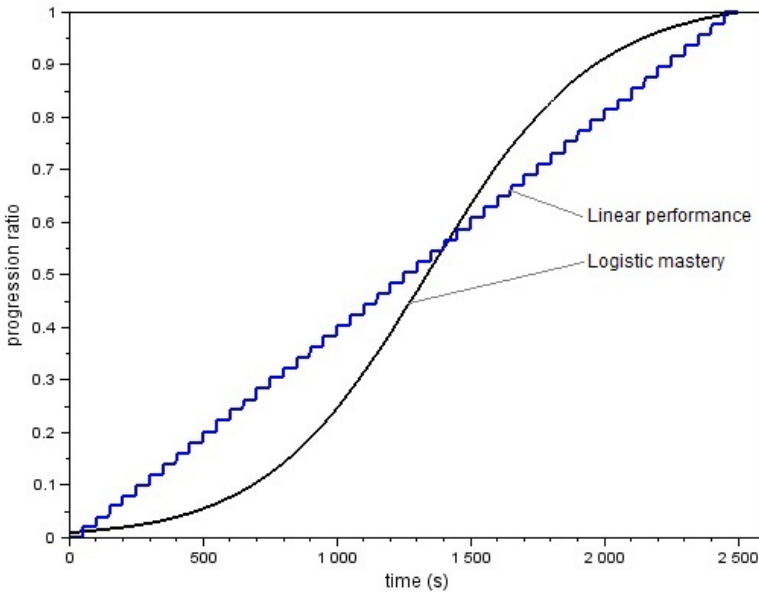
$$RM_{\text{progression},t} = \frac{M_t}{M_N} \quad (7)$$

which indicates the player's progression at each step i toward the final (target) mastery level. Likewise, the progression ratio for the linear performance at challenge i is written as

$$RP_{\text{progression},i} = \frac{P_i}{P_n} \quad (8)$$

Figure 3 shows the progression ratios for logistic mastery and linear performance, respectively, as a function of time.

Figure 3 Progression ratios with respect to the final achievement level for logistic mastery (fluent curve) and linear performance (staircase line), respectively, based on 500 simulated game runs for the baseline case (cf. Table 1)



A low value of the progression ratio signals that the player still has a long way to go. The staged performance curve reflects the discrete nature of assigning scores only after completion of each challenge. The figure shows that linear performance initially tends to overrate the player's achievements, which is then compensated for during the final stages of the game, when levels of substantial mastery are reached. The progression ratios only reflect the distance to the final level, but do not necessarily reflect the quality of work so far. Hence, an additional metric is needed to cover this.

5.4.2 The efficacy ratio

The quality of achievement so far is expressed by the efficacy ratio, which is defined as follows for the mastery model

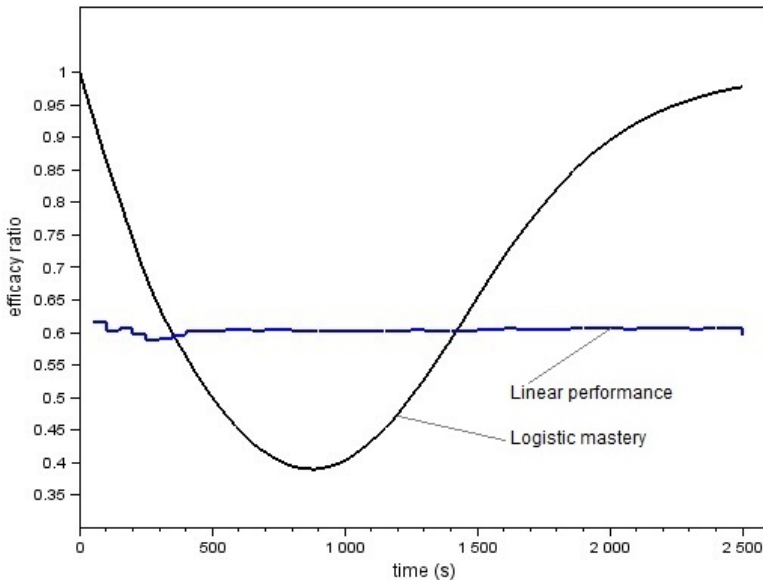
$$RM_{efficacy,t} = M_t / M_{max,t} \quad (9)$$

The progression ratio relates the player's achievements at time t to the best possible achievement level that the player could have reached at time t , rather than to the final target level M_N . It is the fair ratio of the actual achievement M_t and the optimum achievement $M_{max,t}$ with M_{max} being the curve of successes only. The analogous formula for the linear performance efficacy ratio after challenge i reads

$$RP_{efficacy,i} = P_i / P_{max,i} \quad (10)$$

where $P_{max,i}$ is the curve of maximal performance (all successes). Figure 4 shows the efficacies for both models.

Figure 4 Efficacy ratios for logistic mastery (fluent line) and linear performance (staircase line), respectively, based on 500 simulated game runs of the baseline case (cf. Table 1)



While the efficacy for the linear model gravitates around a stable level (given by the challenge success rate $S=0.60$), the logistic model show a profound dependency on time. This is the direct consequence of the exponential growth occurring at low mastery levels: every early failure disproportionately reduces the cumulative growth as compared to the optimal achievement. In the course of time, however, when the optimal achievement curve starts to saturate, the arrears are being overtaken. This metric is thus informative about the quality of work so far as compared to what could have been achieved at this stage. It does not tell anything about the remaining distance to the final level M_N , which is covered by the progression ratio as explained before.

5.4.3 The efficiency ratio

The efficiency of achievements is given by the time spent so far compared to the minimum time (or number of steps i_{\min}) required for having successes only, which can be expressed as follows:

$$RM_{efficiency,i} = \frac{t_{\min}}{t} = M_{\max,i}^{-1}(M_i)/t \tag{11}$$

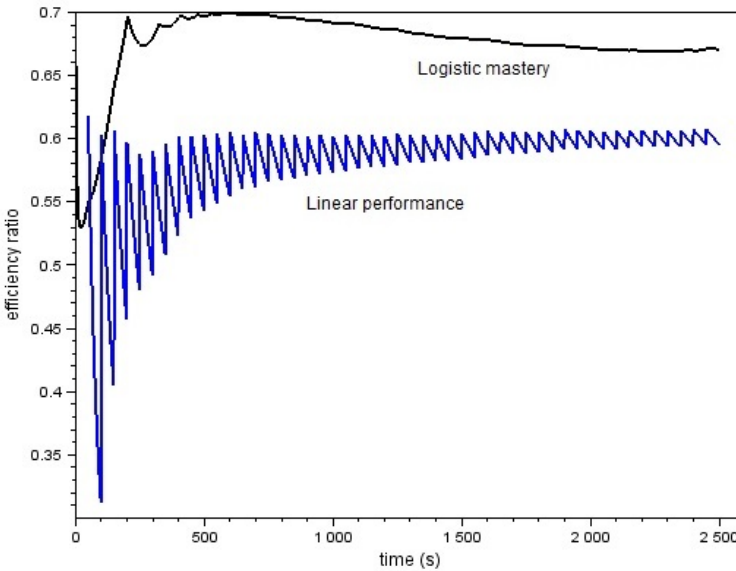
and similarly for linear performance after challenge i

$$RP_{efficiency,i} = \frac{i_{\min}}{i} = P_{\max,i}^{-1}(P_i)/i \tag{12}$$

In equations (11) and (12), M^{-1} and P^{-1} denote inverse functions.

Figure 5 shows the two efficiency ratios.

Figure 5 Efficiency ratios for logistic mastery (fluent curve) and linear performance (sawtooth), respectively, based on 500 simulated game runs for the baseline case (cf. Table 1)



The efficiency ratio of the average performance repetitively touches on the success rate level ($S=0.60$), but decreases hyperbolically during the dead times of challenge execution, since performance scores are assigned only after completion of the challenge. The non-linear skew of the logistic model causes the efficiency ratio to strongly deviate from the efficacy ratio (cf. Figure 4). The efficiency ratio of the logistic model tends to be systematically higher than the ratio for the linear mode. This can be explained by the average growth factor (cf. equation (5)), which predicts a final efficiency level for the baseline case of 0.68. Overall, the linear model systematically underestimates the player's efficiency.

5.5 Influence of growth rates α , β and success rate S

As the effective growth rate of the logistic model is given by equation (5), both α , β en S affect the shape of the resulting growth curves. When β approaches α , which means that the quality of learning from mistakes approaches the quality of learning from successes, the logistic growth will be faster (cf. equation (5)), whereby the logistic progression ratio (cf. Figure 3) will start to exceed the performance progression ratio at an earlier stage. The opposite happens when β gets smaller. For the logistic efficacy ratio, the same holds: when β approaches α , the efficacy goes up, which leads to a radically less pronounced dip in the curve (cf. Figure 4). Likewise, the logistic efficiency ratio goes up, while the linear performance efficiency ratio remains unaffected.

Similarly, a raised success rate S leads to higher growth rates, procuring the same effects, be it, however, that now the performance efficacy ratios and efficiency ratios no longer remain unaffected, but increase as well. The linear progression ratio remains unaffected as a result of the enforced calibration of final performance to the final mastery level. Overall, the exploration with different values for α , β en S show consistent outcomes that entail either less-pronounced or more-pronounced differences between logistic curves and linear performance curves. We wish to emphasise that we have only described here tendencies of behaviours that are averaged over a large number of simulated game runs. Individual play sessions could deviate considerably from the average behaviours (cf. the edgy curve in Figure 2).

6 Study 2: the playground game case study

To further explore the model's behaviours with real-world data, log file data obtained from the Playground game were used (Westera et al., 2014). The Playground game deals with statistics, a domain infamous among university students because of its inherent complexity (Beurze et al., 2013; Griffith et al., 2012). The game offers students a situated problem to get acquainted with statistical concepts and their practical significance. The player's task in the game is to decide upon the most suitable location for laying out a children's playground in a fictitious town, while taking into account a variety of factors and data. The starting point of the game is a research report written by a 'consultant'. This report, however, contains deliberate flaws and fallacies, some of which are manifest and some of which are obscured or subtle. The player's task is to judge the correctness of the approach and the validity of the outcomes by interrogating both the consultant who is the author of the report, and a contra-expert who criticises the report – both represented in interactive videos. The game is structured along eight problem areas surfacing in the consultant's report, which the players can address in arbitrary order. For each problem area a set of challenges is offered, all requiring well-considered decision taking. The game's score system assigns bonus points for each correct decision. The Playground Game is a web-based game, a demo-version of which (in Dutch) is available online at: <http://goo.gl/mwH9YL>.

6.1 *Data collection and processing*

The game was administered to psychology students from the bachelor programme of Leuven University. It was combined with a post-questionnaire composed of 28 items concerning the players' appreciations, judgements about the game, but importantly also including 1) a self-assessment, 2) a set of questions about familiarity with statistical concepts and 3) a set of five methodological test questions, which were combined into an aggregated metric reflecting the post-game mastery level. Out of 125 subscriptions, 117 participants completed the game and questionnaire. The anonymised log files of students were filtered to identify the key events, in particular, the timestamps of each game challenge and the awarded scores. This way, the game data represented a chain of subsequent challenges and the associated successes and failures, which is in agreement with the frugal model.

The session times were typically 1 hour (standard deviation 53 minutes), showing large variability at the high end. Performances were based on the in-game scoring model (assigning 1 point for a success) and rescaling these by enforcing the final performance to equal the post-game test outcome. Model computations were carried out with time steps Δt of 1 second, the initial mastery level set to 0.01 and the ratio of failure growth rate and success rate β/α set to 0.2 (in accordance with the baseline model). Equating the final mastery level that a student attained with the test metric from the questionnaire allowed to estimate the growth rates α and β for each student. This was done by first estimating seed values of α and β from the alignment of an analytical solution with the test score, and then subsequently refining the numerical solution with a difference reduction metric (tolerance $< 1\%$).

6.2 *Case results*

For each participant, the log file data were used to calculate the performance curve and the knowledge mastery curve. Figure 6 shows both curves as a function of time, averaged over the population. Although the resulting curves seem to confirm the general pattern obtained from the simulations that the performance scores most of the time exceed the mastery scores (cf. Figure 3), the curves are deceptive because they do not take into account the different session times of participants: at each point in time different players will be at different stages in the game. Consequently, it means that that pool of participants gradually decreases with time, because more and more players will have completed and exited their session. The time axis in Figure 6 is cut off at 5733 seconds, the ultimate point in time that a minimum of 16 players is preserved in the game.

To allow a more appropriate comparison across the pool of participants the different time scales were rescaled to match a fix standard covering each participant's full session. Figure 7 shows the average performance curve and knowledge mastery curve mapped onto a reference scale of 10,000 units: it represents the average patterns of progression toward completion of the game, irrespective of true time.

Figure 6 Average performance (bold solid line) and knowledge mastery (thin line) for the Playground game participants as a function of time

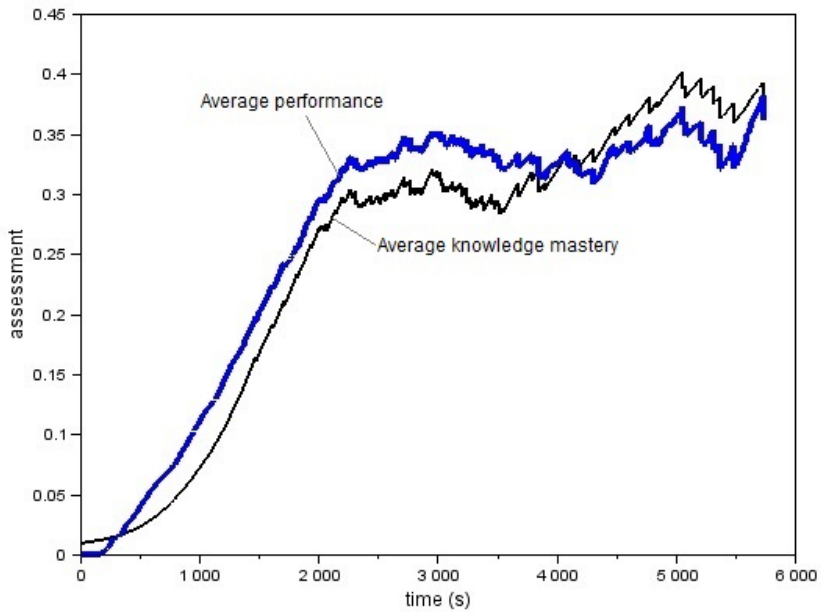
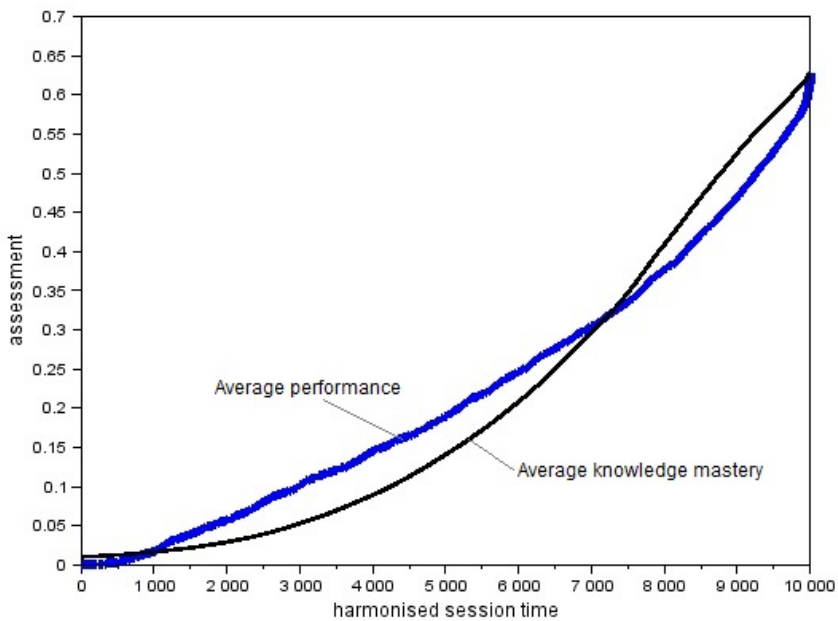


Figure 7 Average performance (bold solid line) and knowledge mastery (thin solid line) of the Playground population aligned to a reference time scale of 10,000 units



These harmonised curves show quite good agreement with the pattern displayed in Figure 3: performance levels tend to exceed the mastery levels for the larger part from the start, which is then compensated for toward the end. A slight deviation from the simulation-based pattern may be observed in the increasing rather than constant slope of the performance curve, which suggests that the time to successfully complete a challenge gets shorter toward the end of the game. This might be explained by the players becoming more knowledgeable about the game's content during the session, which procures faster achievement of successes. Such a mechanism is not assumed in the proposed computational model, but may be easily added if challenge complexity data were available.

The average growth rate for successes (α) was found to be 0.0028 per second with a large standard deviation of 0.0013 s^{-1} . Given the pre-set value of $\alpha/\beta = 0.2$, the corresponding rate for failures (β) is 0.0014 s^{-1} (standard deviation 0.0007 s^{-1}). Logarithms of the individual growth rate α and game session times showed substantial, significant correlation (Spearman's $\rho = -0.88$). This is consistent with the fact the session time was used for deriving an estimated seed value for α . From linear regression the following hyperbolic relationship was derived, using α as a predictor for session time T in this game:

$$T = \frac{8.67}{\alpha} \quad (13)$$

Further correlations were found between players' average challenge duration and session time ($\rho = 0.79$, slope=56.2, intercept=616 (s)), between average challenge duration and growth factor α (log-log: $\rho = -0.66$, log slope=-0.66 (s^{-2}), log intercept=-3.44 (s^{-1})) and, be it less pronounced, between the fraction of time spent to successes and growth factor α ($\rho = -0.48$, slope=-0.0035 (s^{-2}), intercept=0.0047 (s^{-1})).

7 Discussion and conclusion

Model exploration has demonstrated that the differences between common performance metrics and logistic models of knowledge mastery are substantial. Discrete, challenge-based performance metrics, which are used in many serious games, tend to overestimate the player's knowledge mastery at early stages and underestimate it by the end. Although the study was inspired by the idea of learning from mistakes, the differences remain when this factor is excluded ($\beta = 0$), be it less pronounced. Evaluation of three assessment metrics describing progression, efficacy and efficiency, respectively, revealed structural differences between linear performance and logistic mastery. Empirical testing with real-world game data showed results that are largely consistent with the results from Monte-Carlo simulation. Various correlations were identified, most notably the hyperbolic relationship between session time and knowledge growth rate α . Since the latter may be regarded as a stable personal characteristic (within a given domain), it may act as a personal predictor of session time (speed). Application of the model in other games would require tuning of the (baseline) model parameters to the particular game at hand. Initial knowledge mastery levels of participants (M_1) may be available from prior

tests, the number of challenges (n) are known from the game, and the challenge durations (D_i) and challenge success rates (S_i) can be logged for each participant. The total number of time steps (N) and time increments (Δt) can be set freely, be it that both larger N and smaller Δt would yield higher accuracy, at the expense of processing time. Success growth rates (α) and failure growth rates (β) for each participant may either be estimated or be derived as dependent variables from model evaluations.

This study being positioned as an early exploration of the topic is not without limitations. The presented model provides an unmistakably simplified representation of serious game environments, and could be adjusted and elaborated to meet further requirements. First, it treats knowledge as a single scalar, while in practice multidimensional competency constructs may be needed. If the superposition principle applies, however, this multidimensionality need not be a fundamental issue. Second, the model uses the dichotomy of successes and failures. It may need extension to more detailed scales. Third, the approach so far assumes that the game challenges are exchangeable and independent. In practise, game challenges may be of different complexity and they are likely to be conditionally dependent requiring a preferential sequence order possibly enforced by narrative. Although accounting for this would require considerable model extension, it would not be a principle problem. Fourth, the model assumes uninterrupted learning of stable intensity at every stage of the game by neglecting any periods of concentration flaws, persistent failure, mood changes, pauses, interruptions or any unproductive action such as navigation. Finally, the assumption that the processes of learning can be adequately described by a logistic growth model would need further investigation, including a well-controlled set-up that allows for frequent, monitoring of knowledge mastery.

Nevertheless, this study has shown that differences between performance and knowledge mastery cannot just be neglected. Linear performance models may be well suited to assess correctness and fluency of task execution and the associated operational skills, but they are deceptive when equalled with learning and true mastery, in particular because they neglect the underlying factors of understanding, deep processing and reasoning. The ideal student completing the game quickly without errors may have learned less than the slow, cautious and reflective learner that frequently fails but sturdy reconsiders and gradually recovers. Linear performance metrics are simply based on milestone snapshots, but disregard the concept of growth. The logistic model fully embodies the concept of growth and thereby it possesses a more robust theoretical grounding, which goes beyond the pragmatics of performance assessment. With respect to the research questions stated in the introduction section, we conclude the following. The difference between performance and learning in games can be adequately covered in a formal model. The model assumes non-linear growth of the player's knowledge mastery (in our case logistic growth) and uses a simplified high-level representation of the game as network of game challenges. The model was empirically validated by comparing its outcomes with real-world game data. The model allows for exploring how the difference between performance and learning varies with different model parameters, such as, knowledge growth rate, challenge success rate, error rate, etcetera. A principal conclusion is that the differences between performance and learning are substantial indeed, and dependent on the stage of the learning process. As a consequence, learning and performing in games should be treated differently. This is particularly relevant for the game score systems that are used. These should reflect learning achievements rather

than performances, e.g. the improvement of performance over time would be a more appropriate growth indicator than absolute performance. To truly support the learning, scoring systems should best avoid penalties for making mistakes, should reward error correction positively and should provide sufficient feedback on failure.

Finally, the relevance of the work goes beyond the particular model presented in this study, in that it extends and complements the field of educational research with computation methods that allow for recreating observed phenomena and manipulating these by varying contextual parameters and constraints (De Marchi, 2005). Computational models like the one presented in this article are part of modern systems theory, which combines system dynamics (the holistic study of social systems), dynamic systems (mathematically grounded models, largely originally from engineering and exact sciences), with the opportunities of ever-growing computing power (Osipenko and Farr, 2004). Computational modelling methodologies are likely to positively contribute to enhanced learning theory formation and testing, enhancing the explanatory and predictive power of educational research, and to anticipating the ever-growing opportunities for data-driven research methodologies in the digital era.

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